- We thank all three reviewers for their comments, which we respond to below.
- Reviewers 2 and 3 ask about the comparison to the prior mean estimation work of Feldman and Steinke [8] and the
- 3 truncation/global sensitivity approach of Karwa and Vadhan [15]. We agree that a more detailed comparison to these
- 4 works is needed and we will add this to our paper. We briefly describe the advantages of our approach now.
- 5 In short, our algorithm is applicable to a wide variety of distributions, whereas the prior works lack this versatility.
- 6 The truncation/global sensitivity approach of Karwa and Vadhan works for light-tailed distributions like the Gaussian.
- 7 However, the accuracy rapidly degrades if the distribution has heavier tails (e.g., a Student's T distribution or a log-
- 8 Normal); the truncation interval must be very large to avoid biasing the output, but this results in high global sensitivity
- 9 and thus more variance due to added noise. Our trimming approach is much more resilient to heavy tailed distributions
- without sacrificing anything in the ideal case where the distribution is light-tailed.
- We also consider global sensitivity as a comparison point in our experimental evaluation. (This is the flat line in the
- plots.) The relative performance depends on the truncation interval [a, b]. For the given parameters, smooth sensitivity
- 13 performs much better.
- On the other hand, the median-of-means approach of Feldman and Steinke is more resilient to heavy tails. However,
- their approach cannot adapt when the distribution is well-behaved. For example, if the data is Gaussian, then our
- algorithm attains near-optimal accuracy per Theorem 6, whereas their algorithm cannot asymptotically match this level
- of accuracy for any setting of its parameters.
- 18 We remark that our results for differential privacy are actually formally incomparable to those of Feldman and Steinke.
- 19 Their results are in the context of adaptive data analysis, rather than privacy. In particular, they do not provide a
- 20 comparable theorem statement and the algorithm is only implicit in their work. Thus the comparison we draw in this
- 21 discussion is based on our interpretation and analysis of their approach, rather than their stated results.
- Generally, our approach can handle heavy or light tails with ease because the trimming automatically adapts to the distribution (unlike truncation).
- We will clarify these points in the paper by adding a theorem statement covering classes of distributions for which our approach greatly outperforms both prior approaches e.g., heavy-tailed symmetric distributions, such as the Student's T.
- Reviewer 2 asks about other uses of the smooth sensitivity framework. We describe a few examples in the related work section. (Since the NeurIPS submission deadline, two further papers have appeared that apply the smooth sensitivity framework to median estimation and to estimating the degree distribution of a graph.) Implementing these is beyond the scope of our current work.
- We remark that the adoption of smooth sensitivity in applied work has been hampered by a few factors. One is computational intractability for many problems, as noted by Reviewer 1. Another is the fact that the existing noise distributions are unwieldy either they have very heavy tails or a $\log(1/\delta)$ factor appears in their scale which can be fatal in practice. Our work addresses this situation by studying a fundamental building block (mean estimation) in the design of differentially private algorithms for which computational intractability is not an issue, and by introducing noise distributions with better properties.
- Reviewer 1 asks about Rényi differential privacy (RDP) and the comparison to the work of Papernot et al. using
 Gaussian noise for smooth sensitivity under RDP. Our results are immediately applicable to RDP and we will add an
 explicit discussion of this. In particular, CDP is equivalent to an infinite family of RDP guarantees which we will state
 formally in the next version of the paper.
- The RDP analysis of Gaussian noise in the work of Papernot et al. is similar to that for tCDP, which we already include in our experimental evaluation as a comparison point. RDP potentially yields tighter constants in the analysis, relative
- to tCDP. Since our experimental results suggest that Gaussian noise is not very promising, we did not investigate it
- 44 extensively.