We thank the reviewers for their time and feedback. We address the main concerns raised by different reviewers below.

2 Reviewer 1

- 3 We will provide more illustrations on simple data-sets. As our first goal was to provide a tight analysis of local-sgd
- 4 from a theoretical perspective, we did not highlight the experiments, some are provided in the Supplementary Material.
- 5 We will add an illustration of the optimal behavior described on lines 343-357, and a direct illustration of Corollary 4.
- While not directly illustrative of our theory, experiments in related papers like [1], [2] (which focus on practical aspects)
- 7 are consistent with our findings, and underline similar observations.

8 Reviewer 2

- 9 Thank you for your detailed feedback and precise comments!
- We will further clarify the discussion about functional convergence and also present it earlier. We will also add the
- suggested references and minor changes to the final draft.
- Thank you for the suggestion regarding Assumption A3, which is indeed a bit technical: we will simplify its description
- 13 as you suggested!

14 Reviewer 3

- 15 We would like to point out that the reviewer's major criticism is already tackled in our paper. We offer results both with
- and without the quadratic assumption (Q1): while Theorem 3 uses the Q1, Proposition 1,2 and Theorem 6.2 do not
- 17 require this assumption.
- 18 Especially, Theorem 6.2 which is one of the main contributions of the paper, does not use Q1, but only the more
- 19 common smoothness assumption. The propositions leading up to this theorem (placed in the appendix due to lack of
- space), as well as the online setting's results (Proposition 7) also do not make this assumption.
- 21 We chose to first provide and describe results under Q1 in the main paper only for the sake of brevity, and because they
- 22 convey a very similar message more elegantly, and help to understand our approach.
- 23 We hope this clarifies the reviewer's main concern and that the score will be updated to reflect this.

24 References

- 25 [1] T. Lin, S. U. Stich, and M. Jaggi. Don't Use Large Mini-Batches, Use Local SGD. 2018.
- ²⁶ [2] J. Zhang, C. De Sa, I. Mitliagkas, and C. Ré. Parallel SGD: When does averaging help? 2016.