- 1 The reviewers have raised five issues:
- 2 Testing other architectures
- 3 The most interesting architectures, in our view, are locally connected but *non*-convolutional networks, like those in the
- brain. We are working on tests of this type, but there are technical hurdles, as large non-convolutional networks are still
 extremely slow on computers. We will also investigate training AlexNet and VGG architectures using our approaches.
- 5 extremely slow on computers. We will also investigate training AlexNet and VGG architectures using our approaches 6

7 Figures of experiments where Sign-Symmetry achieved its best results

- 8 We will show these plots in a new Appendix.
- 9
- 10 Alignment

In Figure 4, KP kept matrix and δ angles smaller than WM did, but that may not be the case in all learning tasks. With KP, B converges to \mathbf{W}^T at a rate that depends on λ , the weight-decay factor in equation (17). A big λ speeds up alignment, but may hamper learning. So the question is whether we can find a good balance between weight decay λ and learning rate η_W , but at present we have no mathematical proof that a good balance will always be possible. In this respect, WM may be more versatile than KP, because if mirroring ever fails to yield small enough angles, we can simply do more mirroring, e.g. in sleep.

17

18 Computational costs

¹⁹ Suppose layers l and l + 1 are fully connected, with n_l and n_{l+1} forward units (and the same numbers of feedback ²⁰ units if they are separate from the forward ones), and let $n = min(n_l, n_{l+1})$. Then for each training example, KP does ²¹ $n + 4n_ln_{l+1}$ flops to adjust \mathbf{B}_{l+1} using equation (17). WM does the same number to adjust \mathbf{B}_{l+1} using equation (7) ²² and weight decay. But WM also has to generate a random vector y_l and then perform about $2n_ln_{l+1}$ flops to compute ²³ y_{l+1} from y_l using equation (1), whereas KP uses the same y_l and y_{l+1} that train the forward matrices. In short, WM ²⁴ needs twice as many forward passes as KP does to collect as many training examples for its **B** matrices (whether the ²⁵ net is fully-connected or not).

In our ResNet-18 and ResNet-50 tests, the computational costs of WM's additional forward passes were 1.8 GFLOPs
 and 3.8 GFLOPs respectively, not counting the costs of random number generation.

29 *Could the brain have one-to-one wiring between forward and feedback neurons?*

30 Getting that one-to-one correspondence is of course trivial if the *same* neurons make up the forward and feedback paths,

though then we face the new problem of signal segregation — explaining how signals y and δ can flow through the

same cells without interfering. Some possibilities are that neurons segregate y and δ by conveying them with different

intracellular messengers or computing them in different parts of the cell [22,29], or by multiplexing [23], or by taking

- turns carrying one or the other signal.
- ³⁵ If the forward and feedback paths are *distinct* sets of neurons, then the one-to-one connections might arise during
- development. We know that very precise and consistent neuronal wiring is found in simple organisms such as C. elegans
- and in the compound eyes of insects, while in primate cerebellum there is a mechanism (not fully understood) that wires
- ³⁸ up each Purkinje cell with exactly one appropriate climbing fiber.
- And finally, something less than strict one-to-one wiring may suffice for effective learning. As in the case of weight transposes, an approximate one-to-one wiring might be achieved by simple local learning rules.
- We agree with the reviewer that this question is important, and we now address each of these options for circuitry arrangement in an extended paragraph in the updated manuscript.
- 43 *References*:
- 44 [1]-[28] In main text.

[29] BA Richards, TP Lillicrap, *Dendritic solutions to the credit assignment problem*, Current opinion in neurobiology
 54, 28-36.