We thank the three reviewers for their constructive comments. The following are our responses to reviewers’ comments.

---To Reviewer #1---

Re. the notion of orthonormality: When we designed our method, we followed the original forms of existing metric learning models and thus did not use the additional orthonormality constraints. Actually, metric learning aims to find embedding directions (see Fig. 1 in our paper) so that the resulting metric can faithfully preserve the intrinsic distances of data pairs. The directions with necessarily high variations for the subsequent classification are usually favored by many dimension reduction techniques such as PCA.

Re. simplifying derivations and proofs: As the reviewer suggested, in the final paper, we will try our best to simplify the derivations of gradients, and carefully expand the proofs to make them easier to understand.

Re. the complexity, runtime, and code release: The matrix multiplication complexities of Eq. (14) and Eq. (16) are \(O(c^2hmd)\) and \(O(Lchmd)\), respectively. Here \(h\) and \(d\) are the batch-size and data dimension correspondingly, and the constants \(c\) and \(L\) are independent of the size of datasets. Since the measurer line number \(m\) is always set to be smaller than \(d\), the total complexity of our algorithm is \(O(hd^2)\), which is the same as most of the baseline methods. The results of CPU hours (Core Duo 2.93GHz desktop with 16G RAM) on MVS dataset (10^5 training pairs and 10^4 test pairs) are presented in Table II which show that our method requires comparable runtime with existing methods. We will release the code if this paper is accepted.

---To Reviewer #2---

Re. the interpretation should be regarded as a good motivation: Thanks for your suggestions. We will modify our claim on interpretation (i.e., Line 101) from the viewpoint of motivation, “which might be more intuitive than the previous interpretations.” —→ “which offers a clear way to handle the nonlinear data with geometric structures.”

Re. more recent baselines and DDML training details: As the reviewer suggested, we add new experiments for comparing the baseline methods “Npairs Loss” and “Angular Loss” reported in “Making Classification Competitive” (CVPR 2019) and “Hardness-Aware Deep Metric Learning” (CVPR 2019) for further comparisons. The six classification datasets and three verification datasets in our paper are used here. Table III lists the error rates on classification tasks (“∗” denotes a significantly better result at the significance level 0.05) and AUC values on verification tasks for various methods. Obviously, our CDML outperforms the recent baselines in most cases. We believe that the above new results further improve the fairness and sufficiency of our experiments, and we will duly add them in our final paper. For the training of DDML details, the regularization parameter \(\lambda\) was tuned via searching the grid \(\{10^{-2}, 10^{-1}, 1, 10, 10^2\}\) by observing the model performance on validation set. Other configurations such as network architectures, weight initializations, and SGD-related parameters were set as recommended by the authors of “Discriminative Deep Metric Learning for Face Verification in the Wild” (CVPR 2014).

---To Reviewer #3---

Re. the solution and Theorem 2/3: The theoretical analyses on generalization bound usually focus on the ideal case when the globally optimal solution is obtained, although the models are nonconvex such as “Learning Latent Space Models with Angular Constraints” (ICML 2017) and “Fast Generalization Error Bound of Deep Learning from a Kernel Perspective” (ICML 2018). We thus follow such common practice and also discuss the ideal case in our theoretical analysis. The globally optimal solution might not be acquired by our method practically due to the non-convexity of objective function, and this practical phenomenon is also observed in above prior works.

Re. discussing tensor \(\mathcal{A}\) and function \(B(\lambda)\): The tensor \(\mathcal{A}\) is predefined to smooth and stabilize the learning of polynomial coefficients. We can treat it as a constant which restricts the high variations of the learning parameter \(\mathcal{M}\) within a small hypothesis space. In our experiments, \(\mathcal{A}\) is simply fixed to 0, i.e., using the original Frobenius-norm regularizer. For the function \(B(\lambda)\), its expression has been shown in Eq. (B.14) in supplemental materials as

\[
B(\lambda) = 2E_{x,z} (\sup_{\mathcal{M} \in \mathcal{F}(\lambda)} \mathbb{E}_{\mathcal{M}}(\mathcal{M}) - \mathbb{E}_{\mathcal{M}}(\mathcal{M})) / E_{x,z} (\sup_{\mathcal{M} \in \mathcal{F}(\lambda)} \mathcal{M} - \mathcal{Z}(\mathcal{M})).
\]

This expression reveals that when the regularization parameter \(\lambda\) increases, the hypothesis space \(\mathcal{F}(\lambda)\) shrinks, so the numerator in the above expression decreases (the denominator does not change as it is irrelevant to \(\lambda\)), which further leads to a smaller \(B(\lambda)\) and a tighter upper bound. We will add the above discussions in the final paper.

Re. declaration for “supervised metric learning”: Thanks. We will carefully declare that our paper focuses on supervised metric learning in the Introduction section.