Response to reviewers for the paper: “On Lazy Training in Differentiable Programming”

We thank the reviewers for their comments and suggestions. Hereafter, we list reviewers’ (sometimes paraphrased) comments (C) followed by our responses (R). Each answer will translate into a clarification in the final version.

Reviewer #2 and #3 felt that our message was lacking clarity. We would like to re-emphasize that our paper is foremost a reaction to a series of papers (some of them published in the main machine learning venues) with strong claims about optimization of over-parameterized neural networks. We point to the fact that these results are due to a default of normalization, which yields a degenerate “lazy” limit that does not describe well the behavior of competitive over-parameterized models. Along the way, we study lazy training in detail, because it is an interesting novel implicit bias phenomenon in non-convex optimization.

Response to reviewer #1’s comments

- (C) It seems that this paper considers both empirical loss and population loss. (R) Our statements indeed apply to any setting where one wants to fit a non-linear model using a convex loss without regularization. In the experiments, we minimize the population loss in Fig 2.b and the empirical loss everywhere else. We will clarify this.

- (C) The authors should provide analysis about the generalization behavior about two-layer neural networks. (R) We would like to maintain our focus on the optimization aspect, which is where lazy training is new. From a statistical aspect, the model behaves like its linearization (see Prop. A.1, up to a $O(1/\alpha)$ error), in this case a random feature model (Sec. A.2). We will add more pointers to their statistical analysis, from the existing literature (e.g. F. Bach, On the Equivalence between Kernel Quadrature Rules and Random Feature Expansions, JMLR 2017) and also from follow up work from other authors.$^1$

Response to reviewer #2’s comments

- (C) What does this analysis tell about over-parameterized neural networks? We reiterate that the lazy behavior of over-parameterized two layer neural networks, discussed in a series of papers (e.g., [11, 21, 10, 2, 3, 36]), is due to an implicit choice of degenerate scaling (cf. L81-90 in the main paper, often $\alpha(m) = 1/\sqrt{m}$ in these works). Instead, we show that with the scaling $\alpha(m) = 1/m$, over-parameterization is unrelated to laziness. We also show that the lazy regime leads to poorer performances, and thus should be avoided (see e.g. Fig. 2.(a)).

- (C) Can any of the experiments in the paper help to compare the behavior of lazy training in over-parameterized vs not models? This is a pertinent comment. We have conducted additional experiments that have shown that even very wide neural networks perform poorly in the lazy regime. We started from a standard CNN (VGG) on CIFAR and widened each layer by a factor 8, implying that the number of parameters was multiplied by roughly $8^3$. Trained in the lazy regime, we obtained the poor performance of 61.7% test accuracy against 89.7% for its non-lazy counterpart, which is consistent with our claims. We will add this result in the final version of the paper.

Response to reviewer #3’s comments

- (C) The paper builds on the existing idea of lazy training. (R) The term “lazy training” is introduced in this paper. Previous works have proved that over-parameterized neural networks could have a lazy behavior, but we are the first to put forward the phenomenon at play (degenerate scaling), to show its generality (beyond over-parameterization and beyond neural networks), its drawbacks (features are not learnt) and how to avoid it (through scaling or initialization).

- (C) Technically, the paper is not strong, it feels more like an experimental paper. (R) We agree that once the notion of scale is isolated, the theoretical results are almost elementary (to the exception of Thm. 2.5, as noted by reviewer #1). This is actually our goal to put simplicity forward and we believe this should rather be considered as a strength.

- (C) The idea is interesting but I am not sure about its importance. (R) To us, this paper is important for two reasons:
  - it mitigates the claim of the series of work on neural networks optimization, which is needed for practitioners to not search for lazy training, and as well for theory of over-parameterization to be explored in other directions;
  - the notion of lazy training explains the behavior of a large class of models in certain regimes of hyper-parameters. Although in this paper, to fix ideas, the scale is explicitly represented by $\alpha$, it translates in practice to the variance of the initialization, the number of neurons or the normalization of the labels, which practitioners have to deal with when defining a model.

$^1$Which we do not cite to preserve anonymity.